**Title:** A parallel, multi-rate finite volume framework for adaptive, logically Cartesian sphere grids

**Authors:** Donna Calhoun (Boise State University, ID), Carsten Burstedde (University of Bonn, Germany)

**Abstract:** We describe a parallel, adaptive, multiblock method for solving conservation laws on a finite volume sphere grid. The grid layout we consider consists of a nested hierarchy of fixed size, non-overlapping, logically Cartesian meshes stored as leaves in a quadtree. Dynamic grid refinement and de-refinement, and parallel partitioning of the grids is done through the use of the highly scalable quadtree/octree based \texttt{p4est} code (C. Burstedde). Because the code is multi-block, we are able to easily solve on a variety of geometries, including cubed sphere and the two-patch sphere grid proposed by Calhoun, Helzel and LeVeque (SIAM Review, 2008). We describe the details for coordinating the multi-rate time stepping strategy with parallel ghost patch exchanges and show that that using a multi-rate time stepping does not impact the parallel performance. We will demonstrate results from benchmark problems described in Lauritzen et al. (Geoscientific Model Development, 2014), using the second order, finite volume wave propagation algorithms for hyperbolic PDEs (\texttt{ClawPack}, R. J. LeVeque).